

### Warm-up:

\*Test Thursday!

1) Solve for x by factoring:  $2x^2 + 3x = 5$

2) Simplify:  $\frac{7+i}{6-i} - \frac{43+13i}{37}$

3) Solve using the quadratic formula:  
 $x^2 - x - 4 = -8$

4)  $f(x) = -2(x+3)^2 - 6$   
Find vertex, focus and directrix

5) Write the Equation of the Circle and identify the center and radius  $x^2 + 12x + y^2 - 14y = 15$

### NC Final Exam Question of the Day

8 The diameter of a circle is 8 centimeters. A central angle of the circle intercepts an arc of 12 centimeters. What is the radian measure of the angle?

A  $\frac{3}{2}$

**B** 3

C 4

D  $8\pi$

$d = 8 \text{ cm}$  arc = 12  
 $\theta$  in radians?  $\pi$  in the num  
 arc length =  $\frac{\theta}{360} \cdot \pi D$   $D \rightarrow R$   $\frac{\pi}{180}$   
 $\frac{12}{4} = \frac{4\theta}{4}$   
 $\theta = 3$

\*\* Series : expression for the sum of the terms of a sequence.

--Arithmetic Series:

n - term #

$a_1$  - first term

$a_n = a_1 + (n-1)d$

need to know 4 things:  $d, a_1, n, a_n$

**Example 2:** Find the sum of each arithmetic series.

a)  $10+7+4+\dots, n=5, d=3, a_1=10, a_n = 10 + (5-1) \cdot 3 = -2$

$S_n = \left(\frac{5}{2}\right)(10 + -2) = 20$

b)  $50+55+60+\dots, n=7, d=5, a_1=50, a_n = 50 + (7-1)5 = 80$

$S_n = \left(\frac{7}{2}\right)(50 + 80) = 455$

notation for series  $\rightarrow S_n = \frac{n}{2}(a_1 + a_n)$

**example 3:** Find the sum of each geometric series.

r - common ratio

a)  $1+2+4+\dots, n=5$

$r=2, a_1=1$   
 $S_n = \frac{1(1-2^5)}{(1-2)} = 31$

b)  $80-40+20-\dots, n=8$   
 $r=-.5, a_1=80$   
 $r = \frac{-40}{80} = -.5$   
 $S_n = \frac{80(1-(-.5)^8)}{(1-(-.5))} = 53.125$

c)  $8-\frac{8}{7}+\frac{8}{49}-\dots+8\cdot\left(-\frac{1}{7}\right)^{2500}$   
 $a_1=8, r=-\frac{1}{7}, n=2500$   
 $S_n = \frac{8(1-(-\frac{1}{7})^{2500})}{(1-(-\frac{1}{7}))} = 7$

d)  $1500 + (1500 \cdot 3)^1 + (1500 \cdot 3)^2 + \dots + (1500 \cdot 3)^{11}$   
 $n=12, a_1=1500, r=3, S_n = \frac{1500(1-3^{12})}{(1-3)} = 398580000$