

# Warm-Up:

1) Write as a single logarithm:

a)  $\log 2 + 3\log x$

b)  $2\log_4 y - \log_4 x$

$\log_4 y^2 - \log_4 x = \log_4 \left(\frac{y^2}{x}\right)$

2) Expand:

a)  $\log_2 x^5 y^2 = 5\log_2 x + 2\log_2 y$

b)  $\log \frac{2x}{y^3} = \log 2 + \log x - 3\log y$

# ACT Question of the Day

18. In which of the following are  $\frac{1}{2}$ ,  $\frac{5}{6}$ , and  $\frac{5}{8}$  arranged in ascending order? ascending - goes from least to greatest

F.  $\frac{1}{2} < \frac{5}{8} < \frac{5}{6}$

G.  $\frac{5}{6} < \frac{1}{2} < \frac{5}{8}$

H.  $\frac{5}{6} < \frac{5}{8} < \frac{1}{2}$

J.  $\frac{5}{8} < \frac{1}{2} < \frac{5}{6}$

K.  $\frac{5}{8} < \frac{5}{6} < \frac{1}{2}$

$\frac{1}{2} = .5$

$\frac{5}{6} = .83$

$\frac{5}{8} = .625$

# NC Final Exam Question of the Day

20 Which expression is equivalent to  $\frac{x+7}{x^2+4x-21} + \frac{x+5}{x^2+8x+15}$  when x is restricted so that the expressions are defined?

A  $\frac{x+3}{x-3}$

B  $\frac{x-3}{x+3}$

C 1

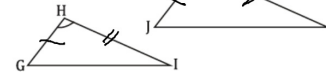
D -1

$\frac{x+7}{(x-3)(x+1)} + \frac{(x+3)(x+5)}{x+5}$

$\frac{-21}{-3 \times 7} \quad \frac{15}{3 \times 5}$

# Review: Triangle Proofs

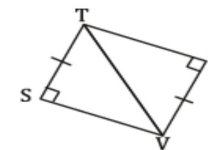
12. Given:  $\frac{GH}{JK} = \frac{HI}{KL}$ ,  $\angle H \cong \angle K$



Prove:  $\triangle GHI \sim \triangle JKL$

Statements	Reasons
1. $\frac{GH}{JK} = \frac{HI}{KL}$	1. given
2. $\angle H \cong \angle K$	2. given
3. $\triangle GHI \sim \triangle JKL$	3. SAS

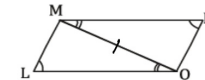
6. Given:  $\overline{ST} \cong \overline{VU}$



Prove:  $\angle SVT \cong \angle UTV$

Statements	Reasons
1. $\overline{ST} \cong \overline{VU}$	1. given
2. $\overline{TV} \cong \overline{TV}$	2. Reflexive Property
3. $\triangle SVT \cong \triangle UTV$	3. HL
4. $\angle SVT \cong \angle UTV$	4. CPCTC

4. Given:  $\angle L \cong \angle N$ ,  $\angle LOM \cong \angle NMO$



Prove:  $\triangle LMO \cong \triangle NMO$

Statements	Reasons
1. $\angle L \cong \angle N$	1. given
2. $\angle LOM \cong \angle NMO$	2. given
3. $\overline{MO} \cong \overline{MO}$	3. Reflexive Property
4. $\triangle LMO \cong \triangle NMO$	4. AAS

## Unit 6 ~ Logarithms & Exponentials

Objective: F.IE.4

$$\begin{array}{l} \text{log form} \\ \log_b x = y \\ \text{exp form} \\ b^y = x \end{array}$$

**Day 4:** logs are the inverse of exp.

# Solving Exponential & Logarithmic Equations

## Solving Exponential Equations:

### Example 1: Solve $256^{2x} = 64$

$$\begin{array}{l} b=256 \quad x=64 \quad y=2x \\ \log_{256} 64 = 2x \\ \frac{\log 64}{\log 256} = 2x \\ \frac{.75}{2} = \frac{2x}{2} \\ x = .375 \end{array}$$

### Example 2: Solve $6^{4x} = 512$

$$\begin{array}{l} b=6 \quad x=512 \quad y=4x \\ \log_6 512 = 4x \\ \frac{\log 512}{\log 6} = 4x \\ \frac{3.48}{4} = \frac{4x}{4} \\ x = .87 \end{array}$$

**HINT:**  
**PUT IN LOG FORM!!**

## Your Turn:

Solve for x.

1)  $27^{3x} = 81$

$$b=27 \quad y=3x \quad x=81$$

$$\log_{27} 81 = 3x$$

$$\frac{\log 81}{\log 27} = 3x$$

$$\frac{1.3}{3} = \frac{3x}{3}$$

$$x = .44$$

2)  $5^{2x} = 130$

$$b=5 \quad y=2x \quad x=130$$

$$\log_5 130 = 2x$$

$$\frac{\log 130}{\log 5} = 2x$$

$$\frac{3.02}{2} = \frac{2x}{2}$$

$$x = 1.51$$

## Solving Logarithmic Equations:

### Example 1: Solve $\log(5x + 2) = 2$

If there is no base... your base is always 10

$$b=10 \quad x=5x+2 \quad y=2$$

$$10^2 = 5x + 2$$

$$\frac{100 - 2}{98} = \frac{5x}{5}$$

$$x = 19.6$$

**Hint:**  
**Put in exponential form!**

### Example 2: Solve $\log 2x^2 - \log 5 = 1$

condense:  $\log \frac{2x^2}{5} = 1$

$$b=10 \quad 5 \cdot 10^1 = \frac{2x^2}{5} \cdot 5$$

$$y=1$$

expanded

$$\frac{50}{2} = \frac{2x^2}{2}$$

$$\sqrt{25} = \sqrt{x^2} \quad x = 5$$