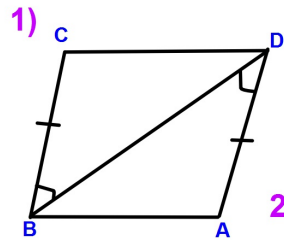


## Warm-up:

Determine how the triangles are congruent.  
Write the congruence statement.

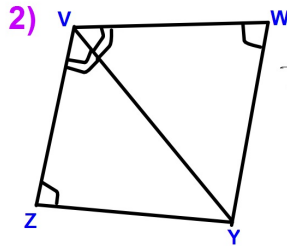


$$\overline{BC} \cong \overline{DA}$$

$$\angle B \cong \angle D$$

$$\overline{BD} \cong \overline{BD}$$

By SAS

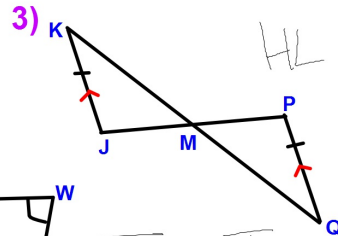


$$\overline{VZ} \cong \overline{WY}$$

$$\angle Z \cong \angle Y$$

$$\angle V \cong \angle W$$

by AAS



$$\overline{KJ} \cong \overline{PQ}$$

$$\angle M \cong \angle M$$

HL

## ACT/SAT Practice:

3) What is the slope of the line  
 $4x = -3y + 8$  ?

$$y = \frac{4x - 8}{-3}$$

$$y = -\frac{4x}{3} + \frac{8}{3}$$

$$m = -\frac{4}{3}$$

18 What is the solution to the equation  $\frac{2x - 3}{x - 1} = \frac{8x + 1}{4x + 5}$  ?

A  $\frac{-14}{5}$

B  $\frac{-14}{9}$

C  $\frac{14}{9}$

D  $\frac{14}{5}$

$$4x \begin{array}{r} 2x - 3 \\ 8x^2 - 7x - 15 \\ \underline{-8x^2 + 2x + 1} \\ -5x - 14 \end{array} \quad x \begin{array}{r} 8x + 1 \\ 8x^2 + 4x - 8x - 1 \\ \underline{-8x^2 + 2x + 1} \\ -5x - 14 \end{array}$$

$$\frac{8x^2 - 7x - 15}{-8x^2 + 2x + 1} = \frac{8x^2 - 7x - 1}{-8x^2 + 2x + 1}$$

$$\frac{-14}{-5} = \frac{-5x}{5}$$

$$x = \frac{14}{5}$$

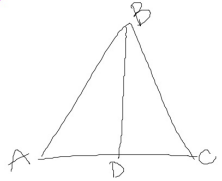
## Unit 5 - Geometry

Objective: G.CO.10

# Day 5 - Congruent Triangle Proofs

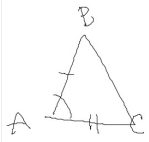
## Useful Properties:

### 1) Reflexive Property - $a \cong a$



$$\overline{BD} \cong \overline{BD}$$

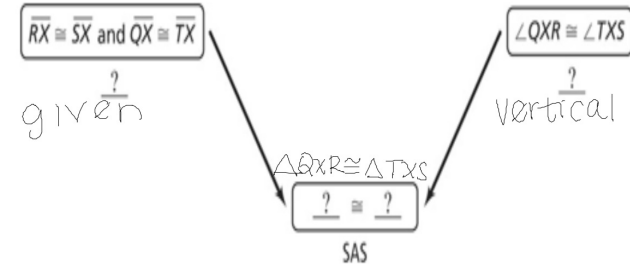
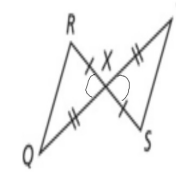
### 2) CPCTC - corresponding parts of congruent triangles are congruent.



$$\begin{aligned} \overline{AB} &\cong \overline{DE} & \triangle ABC &\cong \triangle DEF \\ \angle A &\cong \angle D & & \text{by SAS} \\ \overline{AC} &\cong \overline{DF} & & \end{aligned}$$

## 1) Flow Proof:

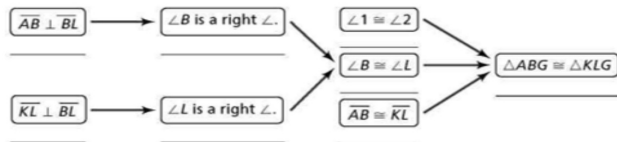
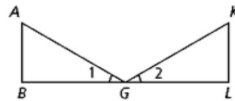
Given:  $\overline{RX} \cong \overline{SX}$ ,  $\overline{QX} \cong \overline{TX}$   
 Prove:  $\triangle QXR \cong \triangle TXS$



## 2) Flow Proof:

Given:  $\angle 1 \cong \angle 2$ ,  $\overline{AB} \perp \overline{BL}$ ,  $\overline{KL} \perp \overline{BL}$ ,  $\overline{AB} \cong \overline{KL}$

Prove:  $\triangle ABG \cong \triangle KLG$

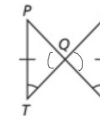


## 3) Two-Column Proof:

Given:  $\overline{PT} \cong \overline{RS}$ ,  $\angle PTR \cong \angle RSP$

Prove:  $\triangle POT \cong \triangle ROS$

1st statement  
last statement

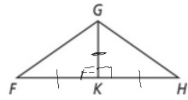


Statements	Reasons
1) $\overline{PT} \cong \overline{RS}$ , $\angle PTR \cong \angle RSP$	1) Given
2) $\angle POT \cong \angle ROS$	2) Vertical angles
3) $\triangle POT \cong \triangle ROS$	3) AAS

4) Two-Column Proof:

Given:  $\overline{GK}$  is the perpendicular bisector of  $\overline{FH}$ .

Prove:  $\overline{FG} \cong \overline{HG}$



$\overline{GK} \cong \overline{GK}$   
reflexive prop.

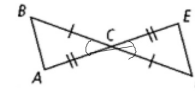
SAS

Statements	Reasons
1) $\overline{GK}$ is the perpendicular bisector of $\overline{FH}$ .	1) given
2) $\overline{FK} \cong \overline{HK}$	2) Def. of perpendicular bis.
3) $\angle GKF \cong \angle GKH$	3) Def. of perpendicular bis: all right $\Delta$ are $\cong$ .
4) $\overline{GK} \cong \overline{GK}$	4) Refl. Prop. of $\cong$
5) $\Delta FGK \cong \Delta HGK$	5) SAS
6) $\overline{FG} \cong \overline{HG}$	6) Corresp. parts of $\cong \Delta$ are $\cong$ .

5) Write a two-column proof.

Given:  $\overline{BC} \cong \overline{DC}, \overline{AC} \cong \overline{EC}$

Prove:  $\Delta ABC \cong \Delta EDC$



$\angle C \cong \angle C$   
vertical angles

Statement	Reason
1. $\overline{BC} \cong \overline{DC}, \overline{AC} \cong \overline{EC}$	1. given
2. $\angle C \cong \angle C$	2. vertical angle
3. $\Delta ABC \cong \Delta EDC$	3. SAS

6) Write a two-column proof.

Given:  $\overline{WX} \parallel \overline{YZ}, \overline{WX} \cong \overline{YZ}$

Prove:  $\Delta WXZ \cong \Delta YZX$



$\angle X \cong \angle Z$   
 $\angle m \cong \angle m$   
V.a

Statement	Reason
1. $\overline{WX} \parallel \overline{YZ}, \overline{WX} \cong \overline{YZ}$ $\angle X \cong \angle Z$	1. given
2. $\angle m \cong \angle m$	2. vertical angle
3. $\Delta WXZ \cong \Delta YZA$	3. AA.S