

Warm-up:

1) $x^2 + 2x$

2) $x^5 + 6x^4$

3) $x^2 + 4x + 4$ $\frac{(x+2)(x+2)}{1 \quad 4}$ Factors of 4
 2 2

5) $x^3 + 8$

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Unit 1 ~ Rationals & Radicals

Objective: A.APR.6

Day 8: Simplifying Rationals

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ACT Question of the Day

4. Given $f = cd^3$, $f = 450$, and $d = 10$, what is c ?

- F. 0.45
- G. 4.5
- H. 15
- J. 45
- K. 150

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Steps:

- 1) Factor the numerator & denominator. on the top
on the bottom
- 2) Cancel common factors.
- 3) Find restrictions.

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Example 1:

Simplify: $\frac{5x^3y}{15xy^3}$

$$\begin{aligned} & \frac{5 \div 5}{15 \div 15} \cdot \frac{x^3}{x^1} \cdot \frac{y^1}{y^3} \\ & \frac{1}{3} \cdot \frac{x^2}{1} \cdot \frac{y^{-2}}{1} \quad \boxed{= \frac{x^2}{3y^2}} \end{aligned}$$

State any restrictions. $y \neq 0$

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Example 2:

Simplify: $\frac{x^2 + 7x + 10}{x^2 - 3x - 10} = \frac{(x+2)(x+5)}{(x+2)(x-5)}$

num $\cancel{x^2}$ Denom $\cancel{x^2}$

$\cancel{10}$ $\cancel{-10}$

$\cancel{2}$ $\cancel{-3}$

factors of 10

$\cancel{2, 5}$

$\cancel{10, 1}$

$= \frac{x+5}{x-5}$

$x-5=0$

$+5 \quad +5$

$\underline{x=5}$

State any restrictions. $x \neq 5$

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Your Turn:

Simplify: $\frac{25x^4y^2}{5x^2y^5}$

$$\begin{aligned} & \frac{25}{5} \cdot \frac{x^4}{x^2} \cdot \frac{y^2}{y^5} \\ & \frac{5}{1} \cdot \frac{x^2}{1} \cdot \frac{y^{-3}}{1} = \frac{5}{1} \cdot \frac{x^2}{1} \cdot \frac{1}{y^3} = \boxed{\frac{5x^2}{y^3}} \end{aligned}$$

State any restrictions. $y \neq 0$

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Your Turn:

Simplify: $\frac{x^2 + 2x - 8}{x^2 - 5x + 6} = \frac{(x-2)(x+4)}{(x-2)(x-3)}$

num $\cancel{x^2}$ Denom $\cancel{x^2}$

$\cancel{-8}$ $\cancel{6}$

$\cancel{-2}$ $\cancel{-3}$

$= \frac{x+4}{x-3}$

$x-3=0$

$+3 \quad +3$

$\underline{x=3}$

State any restrictions. $x \neq 3$

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Example 3:

Simplify: $\frac{2x^2 - 3x - 2}{2x^2 - 8}$

num
 $(2x^2 - 4x)(+x - 2)$ $\cancel{-4}$
 $2x(x - 2) \pm (x - 2)$ $\cancel{2, 3}$
 $(2x + 1)(x - 2)$
Denom
 $\cancel{2}(x^2 - 4)$
 $\cancel{2}(x + 2)(x - 2)$

$$\begin{aligned} &= \frac{(2x+1)(x-2)}{2(x+2)(x-2)} \\ &= \frac{2x+1}{2(x+2)} \\ &= \frac{2(x+2)=0}{2(x+2)} \\ &\quad \cancel{2(x+2)} \quad (x+2)=0 \\ &\quad \cancel{-2} \quad \cancel{-2} \\ &\quad x=-2 \end{aligned}$$

State any restrictions. $x \neq -2$

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Lesson Check

Do you know HOW?

Simplify each rational expression. State any restrictions on the variables.

1. $\frac{4z - 12}{8z + 24}$

2. $\frac{3x - 3}{x^2 - x}$

Example 4:

Simplify: $\frac{(49 - z^2)}{z + 7}$

$$\begin{aligned} &= \frac{(z+7)(z-7)}{z+7} \\ &= \frac{z^2 - 49}{z+7} \\ &= \frac{z^2 - 49}{\sqrt{z^2} = z} \\ &= \frac{\sqrt{49} = 7}{(z+7)(z-7)} \\ &= z-7 \end{aligned}$$

State any restrictions. None

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